# A Curious Artifact in the Potential Energy Surface for the F + HF Abstraction Reaction 

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Received October 26, 1992


#### Abstract

The reaction $\mathrm{F}+\mathrm{HF} \rightarrow \mathrm{HF}+\mathrm{F}$ has been studied using ab initio molecular orbital theory at UHF, MP2, MP3, MP4, CCD, CCSD, CID, CISD, QCISD, QCISD(T), and CASSCF levels of theory with the 3-21G, 6-31G**, $6-311++\mathrm{G}^{* *}$, and D95++(3df,2p) basis sets. The UHF, MP4, CIS, CISD, CCSD, QCISD, QCISD(T), and CASSCF levels of theory predict the transition state to be a highly bent $C_{20}$ symmetry structure, whereas MP2, MP3, and CCD levels predict the $C_{20}$ symmetry structure to be a shallow minimum bound by up to $0.4 \mathrm{kcal} / \mathrm{mol}$. The MP2 $/ 6-31 \mathrm{G}^{* *}$ $C_{20}$ structure is bracketed by two $C_{s}$ symmetry transition states with bond lengths of 1.1411 and $1.0541 \AA$ and a bond angle of $127.0^{\circ}$. The $C_{20}$ minimum on the MP2, MP3, and CCD surfaces is caused by inadequately treated avoided crossings between the bond making/breaking state and two broken symmetry $\mathrm{F}+\mathrm{HF}$ hydrogen bonding states. Dynamic correlation methods that include single excitations in an interative or self consistent manner, such as CASSCF, CISD, CCSD, and QCISD, appear to treat the avoided crossings properly and predict a suitable transition state. At the QCISD(T)/D95++(3df,2p) level, the $C_{20}$ transition state geometry is $R(H-F)=1.102 \AA$ and $\angle \mathrm{F}-\mathrm{H}-\mathrm{F}=134.6^{\circ}$ and the reaction barrier is $17.5 \mathrm{kcal} / \mathrm{mol}$.


## Introduction

Hydrogen atom abstraction reactions, $\mathrm{XH}+\mathrm{Y} \rightarrow \mathrm{X}+\mathrm{HY}$, are of general interest because of their importance in radical chemistry and combustion processes. Recently, hydrogen exchange reactions with $\mathrm{X}, \mathrm{Y}=$ halogen have generated considerable interest in connection with transition state spectroscopy. ${ }^{1}$ Under favorable circumstances, photodetachment of an electron from a bihalide anion, XHY-, can lead to a neutral species with a geometry similar to the transition state for the reaction XH + $\mathbf{Y} \rightarrow \mathbf{X}+\mathrm{HY}$. Neumark et al. ${ }^{2-5}$ found structure in the photodetachment spectra of $\mathrm{ClHCl}^{-}, \mathrm{BrHBr}$, and $\mathrm{IHI}^{-}$, suggesting the existence of vibrational resonances near the transition state. Higher resolution experiments's showed secondary structure in the IHI- spectrum. Schatz ${ }^{6}$ and Bowman ${ }^{7}$ have published detailed quantum scattering calculations and find reasonable agreement with the experimental photodetachment spectra. Morokuma ${ }^{8}$ has suggested that the ${ }^{2} I I$ state could also be contributing to the observed spectra. In contrast to these systems, Neumark ${ }^{9}$ found no structure in the photoelectron detachment spectrum of FHF-. Ault and Andrews ${ }^{10}$ have shown that earlier attempts ${ }^{11}$ to isolate a symmetric, quasistable XHX complex by matrix isolation produced bihalide ions rather than the neutral

[^0]species. Thus, there is no experimental evidence for a symmetric FHF complex and no indication of any vibrational resonances in FHF for geometries similar to FHF-

In early calculations, Schaefer et al..$^{12}$ and Peyerimhoff et al. ${ }^{13}$ obtained barrier heights for collinear F + HF by Hartree-Fock theory and configuration interaction. Vibrational frequency calculations by LeRoy et al. ${ }^{14}$ showed the F + HF transition state to be linear at the HF/4-31G level. More recently, VB-SCF and CAS-SCF calculations ${ }^{15}$ have been used to probe the origin of the barrier for collinear F + HF. There appears to be no high level molecular orbital studies on non-collinear $\mathrm{F}+\mathrm{HF}$ in the recent literature. Calculations on other $\mathbf{X}+\mathrm{HY}$ abstraction reactions have demonstrated that some of these transition states are bent. For example, for $\mathrm{X}=\mathrm{Y}=\mathrm{Cl}, \mathrm{POL}-\mathrm{CI}$ calculations yielded an optimized bond angle of approximately $160^{\circ} .{ }^{16}$ The bending is sometimes revealed only when extensive electron correlation corrections are included. The transition state for the $\mathrm{F}+\mathrm{H}_{2}$ reaction is linear at the HF level but has an angle of approximately $120^{\circ}{ }^{17}$ when a large multi-reference CI approach is employed (however, the potential energy surface is extremely flat with respect to the bending motion). At the highest level of calculations carried out, QCISD(T)/D95++(3df,2p), the F + HF transition state was found to be strongly bent with an angle of $135^{\circ}$.
During a series of investigations of barriers for hydrogen abstraction in X + HY, ${ }^{18} \mathrm{XCH}_{2}+\mathrm{HY},{ }^{19}$ and $\mathrm{XCH}_{2}+\mathrm{HCH}_{2} \mathrm{Y}^{20}$
$(\mathrm{X}, \mathrm{Y}=\mathrm{H}, \mathrm{F}, \mathrm{Cl}, \mathrm{OH}, \mathrm{SH}, \mathrm{CN}$ ), some unusual features were noted and prompted a study of the structure and energetics of the F + HF reaction at levels of theory higher than Hartree-Fock. Of the various methods for including electron correlation, second-

[^1]Table I. Total Energies (au) and Relative Energies (kcal/mol) for Reactants and Transition States

| level | F | HF | FHF | $\Delta E_{\text {rol }}{ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: |
| UHF/3-21G | -98.845 009 | -99.460 219 | -198.258 790 | 29.14 |
| MP2/3-21G | -98.925 143 | -99.583 882 | -198.478 227 | 19.33 |
| QCISD(T)/3-21G | -98.928 312 | -99.586615 | -198.491 931 | 14.43 |
| UHF/6-31G** | -99.364 957 | -100.011 691 | -199.312 236 | 40.42 |
| UMP2/6-31G ${ }^{* *} C_{20}{ }^{\text {b }}$ | -99.489 039 | -100.196700 | -199.654 463 | 19.63 |
| UMP2/6-31G ${ }^{* *} C_{s}$ |  |  | -199.653 792 | 20.05 |
| UMP3/6-31G** | -99.495 693 | -100.196 402 | -199.655 351 | 23.06 |
| UMP4SDTQ/6-31G** | -99.498 652 | -100.201430 | -199.669 626 | 19.11 |
| CAS $(3,3) / 6-31 \mathrm{G}^{* *}$ |  |  | -199.338 988 |  |
| CAS $(7,6) / 6-31 \mathrm{G}^{*}$ |  |  | -199.365 898 |  |
| CID/6-31G** | -99.494 370 | -100.193942 | -199.636709 | 32.38 |
| CISD/6-31G** | -99.495 124 | -100.194892 | -199.645 162 | 28.15 |
| CCD/6-31G** | -99.497088 | -100.198 186 | -199.658 350 | 23.17 |
| CCSD/6-31 G** | -99.497681 | -100.199009 | -199.666 825 | 18.74 |
| QCISD/6-31G** | -99.497954 | -100.199 384 | -199.668 535 | 18.07 |
| QCISD(T)/6-31G** | -99.498983 | -100.201 279 | -199.673 855 | 16.57 |
| UHF/6-311++G*** | -99.399 893 | -100.053 305 | -199.383 339 | 43.84 |
| UMP2/6-311++G** | -99.578 265 | -100.297937 | -199.836 739 | 24.76 |
| CCD/6-311++G** | -99.568 610 | -100.279 123 | -199.803 868 | 27.53 |
| CCSD/6-311++G** | -99.569 512 | -100.280 786 | -199.814 288 | 22.60 |
| QCISD(T)/6-311++G** | -99.571685 | -100.285 333 | -199.825 901 | 19.53 |
| UHF/D95++(3df,2p) | -99.400 961 | -100.054 980 | -199.386 244 | 43.73 |
| UMP2/D95++(3df,2p) | -99.591190 | -100.317007 | -199.872 355 | 22.49 |
| CCD/D95++(3df,2p) | -99.588611 | -100.305 112 | -199.852 738 | 25.72 |
| QCISD( ${ }^{\text {( }) / \mathrm{D} 95++(3 \mathrm{df}, 2 \mathrm{p})}$ | -99.593 039 | -100.312 099 | -199.877 304 | 17.47 |
| PMP2/6-31G**//UMP2/6-31G** | -99.488 228 | -100.196 700 | -199.655 018 | 18.77 |
| PMP3/6-31G**//UMP3/6-31G** | -99.496 116 | -100.196402 | -199.659655 | 20.62 |
| PMP4SDTQ/6-31G**//UMP4/6-31G** | -99.499 075 | -100.201 430 | -199.673973 | 16.65 |

${ }^{a} \Delta E_{\text {rel }}$ is the same as the reaction barrier, $\Delta E^{*}$, for all cases except at the UMP2 and CCD levels. ${ }^{b}$ The well depth at the UMP2/6-31G** level is $0.42 \mathrm{kcal} / \mathrm{mol}$.
order Møller-Plesset perturbation theory, MP2, is used most frequently because of its relatively low computational cost and the availability of energy derivatives. As will be shown below, the $\mathrm{F}+\mathrm{HF}$ transition state is one of a small number of cases where MP2 theory is qualitatively incorrect. It is the aim of this paper to understand the detailed origin of this problem.

## Methods Section

Ab initio molecular orbital calculations were carried out using the GAUSSIAN series of programs. ${ }^{21}$ The $3-21 G, 6-31 G^{* *}, 6-311++G^{* *}$, and D95++(3df,2p) basis sets ${ }^{22}$ were employed to optimize the geometries of the reactants and transition states using Hartree-Fock theory (HF), Moller-Plesset perturbation theory (MP2, MP3, MP4DQ, MP4SDQ, MP4SDTQ), configuration interaction (CID, CISD), coupled clusters methods (CCD, CCSD), and quadratic configuration interaction [QCISD, QCISD(T)], and complete active space multi-configuration self consistent field theory (CASSCF). Analytical gradient techniques ${ }^{23}$ were used for optimization with spin unrestricted HF, MP2, CID, CISD, QCISD, and CAS-SCF levels of theory and a modified Fletcher-Powell optimization method ${ }^{24}$ for the CCD, CCSD, MP3, MP4SDTQ, and QCISD(T) levels of theory. Total energies are listed in Table I and optimized geometries are given in Table II. Some calculations were also carried out with wave functions that are eigenfunctions of spin: complete active space multiconfiguration SCF (CASSCF), restricted open shell Hartree-Fock (ROHF), and restricted open shell second-order Moller-Plesset perturbation theory ${ }^{25}$ (ROMP2). The stationary points on the potential energy surfaces were characterized by vibrational frequency calculations (Table
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Table II. Geometries of F-H-Fa

| level | $\boldsymbol{R}(\mathrm{H}-\mathrm{F})$ | $\angle \mathrm{F}-\mathrm{H}-\mathrm{F}$ |
| :---: | :---: | :---: |
| UHF/3-21G | 1.1277 | 180.0 |
| MP2/3-21G | 1.1126 | 127.7 |
| QCISD(T)/3-21G | 1.1419 | 123.6 |
| UHF/6-31 ${ }^{* *}$ | 1.0943 | 151.5 |
| UMP2/6-31G** $C_{2 v}$ | 1.0873 | 126.1 |
| UMP2/6-31G** $C_{s}$ | 1.0541, 1.1411 | 127.0 |
| UMP3/6-31G** | 1.0896 | 129.6 |
| UMP4SDTQ/6-31G** | 1.0957 | 127.1 |
| CAS $(3,3) / 6-31 \mathrm{G}^{* *}$ | 1.1140 | 180.0 |
| CAS $(7,6) / 6-31 \mathrm{G}^{* *}$ | 1.1110 | 128.7 |
| CID/6-31G** | 1.0884 | 131.5 |
| CISD/6-31G** | 1.0933 | 130.7 |
| CCD/6-31G** | 1.0913 | 129.9 |
| CCSD/6-31G** | 1.1050 | 128.6 |
| QCISD/6-31G** | 1.1064 | 128.3 |
| QCISD(T)/6-31G** | 1.1089 | 127.1 |
| UHF/6-311++G** | 1.0907 | 165.6 |
| UMP2/6-311++G** | 1.0771 | 135.5 |
| CCD/6-311++G** | 1.0819 | 141.8 |
| CCSD $/ 6-311++\mathrm{G}^{* *}$ | 1.0952 | 139.1 |
| QCISD(T)/6-311++G** | 1.0999 | 137.4 |
| UHF/D95++(3df,2p) | 1.0948 | 164.4 |
| UMP2/D95++(3df,2p) | 1.0800 | 130.5 |
| CCD/D95++(3df,2p) | 1.0846 | 136.4 |
| QCISD(T)/D95++(3df,2p) | 1.1023 | 134.6 |

${ }^{a}$ Bond lengths in $\AA$ and angles in deg.
III). Second derivatives were calculated analytically at the HartreeFock level, ${ }^{26}$ by numerical differentiation of analytical gradients for the MP2, CID, CISD, QCISD, and CAS-SCF levels, and by double numerical differentiation of the energy with respect to nuclear coordinates for the MP3, MP4SDTQ, and QCISD(T) levels of theory. The MP2 calculations were performed using all of the occupied and virtual orbitals. For all of the other methods of correlation, the frozen core approximation was employed for the geometry optimizations and frequency calculations. Energy-only calculations at all levels of electron correlation corrections include all orbitals (i.e. not frozen core).

## Discussion

Inspection of the geometries summarized in Table II shows that the transition states calculated at levels of theory other than


Figure 1. Model potential energy surface for $\mathrm{F}+\mathrm{HF}$ fitted to selected MP2/6-31G** energies and derivatives (bending coordinate is in degrees from linearity).


Reaction Coordinate
Figure 2. Potential energy curves at various levels of theory along an approximate MP2/6-31G** reaction path.

Table III. Vibrational Frequencies for $\mathrm{F}-\mathrm{H}-\mathrm{F}^{a}$

| level | $\nu_{1}$ | $\nu_{2}$ | $\nu_{3}$ |
| :--- | :---: | :---: | ---: |
| UHF/3-21G $D_{\infty h}$ | 4322 i | $272(2)$ | 560 |
| MP2/3-31G | 3294 i | 322 | 1911 |
| UHF/6-31G** | 5960 i | 277 | 1162 |
| UMP2/6-31G** $C_{2 v}$ | 493 | 2074 | 3134 |
| UMP2/6-31G** $C_{s}$ | 3404 i | 445 | 2009 |
| UMP4SDTQ/6-31G** | 398 i | 472 | 1978 |
| CAS(3,3)/6-31G ** $D_{\infty h}$ | 4732 i | $287(2)$ | 580 |
| CAS(7,6)/6-31G*** | 9603 i | 474 | 1752 |
| CID/6-31G** | 1399 i | 436 | 1870 |
| CCD/6-31G | 449 | 1913 | 2098 |
| QCISD(T)/6-31G** | 1891 i | 472 | 1848 |
| UHF/6-311++G*** | 6292 i | 235 | 788 |
| UMP2/6-311++G** | 447 | 1800 | 1906 |
| UHF/D95++(3df,2p) | 2677 i | 204 | 820 |
| UMP2/D95++(3df,2p) | 428 | 1895 | 4548 |

${ }^{a}$ In cm ${ }^{-1}$.
UHF/3-21G and CAS $(3,3) / 6-31 G^{* *}$ are significantly bent. The bond angle at the UHF/6-31G** level is $151^{\circ}$, and at correlated levels of theory other than $\operatorname{CAS}(3,3)$, the angle lies in the range of $126-142^{\circ}$. The calculated barriers are ca. $40 \mathrm{kcal} / \mathrm{mol}$ at the Hartree-Fock level and $15-30 \mathrm{kcal} / \mathrm{mol}$ when electron correlation corrections are included. The highest levels of theory employed are in agreement that the transition state geometry is of $C_{2 v}$ symmetry with bond lengths of $1.09 \pm 0.01 \AA$ and a bond angle of $132 \pm 5^{\circ}$. However, the corresponding MP2, MP3; and CCD potential energy surfaces have a small depression centered at the $C_{2 v}$ geometry bracketed by transition states of $C_{s}$ symmetry. The whimsical term "Lake Eyring" has occasionally been used in the vernacular to refer to such a complex or basin in the region of
a transition state. For basis sets of $6-31 \mathrm{G}^{* *}$ quality or better, the minimum at the MP2 level appears to be independent of the quality of basis set. The main focus of this paper is to gain an understanding of the origin of this anomaly.

An approximate potential energy surface has been fit to the energies, gradients, and second derivatives at a suitable set of points computed at the MP2/6-31G** level. As can readily be seen in Figure 1, this surface has a shallow depression along the reaction path centered at the $C_{2 v}$ geometry. Such a characteristic in the surface, if it were real and not an artifact of the theoretical method, would lead to intense interest in both the experimental and theoretical communities todetect the quasistable intermediate and probe the effects of such a minimum on the dynamical behavior. However, as mentioned above, this minimum is not reproduced at higher levels of theory and is an artifact of Møller-Plesset perturbation theory.

To investigate the source of this shallow well, the $C_{20}$ structure of $\mathrm{F}-\mathrm{H}-\mathrm{F}$ was optimized at various levels of theory and characterized by frequency calculations at the same level. The total energies of the reactants, intermediate (at the levels where it exists), and transition states are listed in Table I. The potential energy surfaces at the MP2, MP3, and CCD levels of theory with the $6-31 \mathrm{G}^{* *}, 6-311++\mathrm{G}^{* *}$, and D95++(3df,2p) basis sets exhibit the spurious minima; however, with smaller basis sets (STO-3G, 3-21G, and $4-31 \mathrm{G}$ ) the spurious minimum does not exist. At the CID, CISD, MP4SDTQ, QCISD, QCISD(T), and CAS-SCF levels of theory with all of the basis sets considered, the optimized $C_{2 v}$ structure is a true transition state with one imaginary frequency.

To analyze the effect of the level of theory on the shape of the potential energy surface, a number of calculations were performed along an approximate reaction path obtained from the MP2/ $6-31 \mathrm{G}^{* *}$ calculations. Eleven points along the MP2/6-31G** reaction path were chosen: the MP2/6-31G** optimized $C_{2 v}$ symmetry intermediate, the MP2/6-31G** optimized $C_{s}$ transition states, a linear interpolated point midway between the $C_{20}$ intermediate and each transition state, and three linearly extrapolated points beyond each transition state. The energy profiles calculated with the $6-31 \mathrm{G}^{* *}$ basis set using a variety of electron correlation methods are depicted in Figure 2. The MP2, MP3, MP4DQ, and CCD energy profiles exhibit the spurious minima, whereas the MP4SDQ and MP4SDTQ levels predict the surface to be extremely flat and UHF, CID, CISD, QCISD, and QCISD(T) levels all agree that there is a single transition state along the reaction coordinate.

The first conclusion that one might jump to is that an excited state strongly interacts with the ground state, i.e. sizable nondynamic correlation effects. Perturbation theory handles strong interactions poorly and might lead to the anomalous depression, whereas variational methods treat the interaction properly and reproduce the correct topology of the potential energy surface. This hypothesis can be probed by a simple two-state model. Two limiting cases have been considered: (a) the two states are chosen to have a quadratic dependence on the reaction path and are allowed to interact via a constant matrix element and (b) the energy difference between the two states is fixed and the interaction matrix element is allowed to be quadratic:

$$
\left[\begin{array}{ll}
E_{1} & H_{12}  \tag{1}\\
H_{12} & E_{2}
\end{array}\right]\left[\begin{array}{l}
C_{1} \\
C_{2}
\end{array}\right]=E_{\text {corr }}\left[\begin{array}{l}
C_{1} \\
C_{2}
\end{array}\right]
$$

Case (a): $E_{1}=a+b s^{2}, E_{2}=c+d s^{2}, H_{12}=0.01$
Case (b): $E_{1}=a+b s^{2}, E_{2}=E_{1}+0.003, H_{12}=c+d s^{2}$
In both cases the constants, $a-d$, are determined by fitting the second-order perturbation energy of the two-state system to the ab initio UMP2 energy at seven points along the approximate reaction path. As shown in Figure 3a the choice of $H_{12}=0.01$


Figure 3. Simple two-state model potential energy curves, eq 3, for case (a) with quadratic ground and excited states and constant interaction matrix element ( $H_{12}=0.01$ ) and case (b) with constant energy difference ( $\Delta E=0.003$ ) and quadratic interaction matrix element.
au for case (a) yields a model system in which the second-order perturbation energy has a local minimum at the symmetric structure but the variational energy (CI energy) does not. Likewise Figure 3b demonstrates that the corresponding situation can be obtained for case (b) with $\Delta E=0.003 \mathrm{au}$. Therefore, these simple two-state models suggest that the behavior of the UMP2 surface for $\mathrm{F}+\mathrm{HF}$ could be due to a strong interaction with a low-lying excited state.

To see which interactions could be causing the problems with the MP2 surface, the individual molecular orbitals and their contributions to the correlation energy were examined in more detail. As can be seen in Figure 4, the occupied orbitals involved in the forming and breaking $\mathrm{H}-\mathrm{F}$ bonds are 5 and 8 from the $\alpha$ set and 5 from the $\beta$ set. Note that the in-plane lone pairs on the fluorines mix strongly with the $\mathrm{H}-\mathrm{F}$ bonding orbitals giving rise to orbital $9 \beta$ (the in-plane $\alpha$ lone pairs are relatively unperturbed). The corresponding virtual orbitals related to the H-F bond breaking are $11 \alpha, 12 \alpha, 10 \beta, 11 \beta$, and $12 \beta$.

The contributions to the correlation energy can be partitioned into a sum of pair energies.

$$
\begin{equation*}
E_{\text {corr }}=\sum_{i, j}^{i \neq j} \epsilon_{i j} \tag{2}
\end{equation*}
$$

In the region of the transition state the most important components of the changes in the correlation energy should come from the orbitals involved in the bond making and breaking. Let $E_{2}^{\prime}$ be the contribution of the $(5 \alpha, 8 \alpha),(5 \alpha, 5 \beta),(5 \alpha, 9 \beta),(8 \alpha, 5 \beta)$, $(8 \alpha, 9 \beta)$, and $(5 \beta, 9 \beta)$ pair energies. It can be seen from Figure 5 that $E_{2}^{\prime}$ is in fact the major contributor to the spurious minimum along the MP2 reaction path and that the remainder of the correlation energy, $E_{2}-E_{2}^{\prime}$, is nearly constant in this region. The contributions to $E_{2}^{\prime}$ can be further decomposed by examining which excitations contribute most strongly to the $E_{2}^{\prime}$. Let $E^{\prime \prime}{ }_{2}$


Figure 4. Molecular orbitals involved in the bond making/breaking process: (a) $\alpha$ MO's, (b) $\beta$ MO's.
be the contributions from the symmetry allowed excitations in the active space of the $5,8,11$, and $12 \alpha$ orbitals and $5,9,10$, 11 , and $12 \beta$ orbitals. Figure 6 shows that the excitations in $E^{\prime \prime}{ }_{2}$ account for approximately $90 \%$ of the $\operatorname{dip}$ in $E_{2}^{\prime}$ along the reaction path.

The key contributions to the CID and QCISD correlation energy are defined similar to the MP2 term and are shown in Figure 7. The CID and QCISD contributions mimic the MP2 contribution. The stabilizing effects of the interactions included in $E^{\prime}{ }_{2}$ are, no doubt, responsible for the flattening of the potential energy surface near the $C_{2 v}$ symmetry structure. However, since the differences between the MP2 $E_{2}^{\prime}$ and the CID or QCISD contributions remain nearly constant along the reaction path, this simple explanation cannot be solely responsible for the spurious minimum.


Figure 5. Second-order correlation energy, $E_{2}$, contributions from ( $5 \alpha, 8 \alpha$ ), ( $5 \alpha, 5 \beta$ ), $(5 \alpha, 9 \beta),(8 \alpha, 5 \beta),(8 \alpha, 9 \beta)$, and ( $5 \beta, 9 \beta$ ) pair energies, $E_{2}^{\prime}$, and their difference along the approximate MP2/6-31G** reaction path.


Reaction Coordinate
Flgure 6. Pair energy, $E^{\prime}$, and correlation contributions, $E^{\prime \prime}$, from orbitals $5 \alpha, 8 \alpha, 11 \alpha, 12 \alpha, 5 \beta, 9 \beta, 10 \beta, 11 \beta$, and $12 \beta$ along the approximate MP2/6-31G** reaction path.


Figure 7. Pair energy calculated at the MP2, CID and QCISD levels along the approximate MP2/6-31G** reaction path.

The fourth-order perturbation expansion with only double and quadruple excitations, MP4DQ, exhibits similar behavior to the MP2 potential energy surface, but the addition of single excitations (MP4SDQ) or single and triple excitations (MP4SDTQ) removes the spurious minima along the reaction coordinate. However, the resulting surfaces remain extremely flat near the $C_{20}$ transition state. This is in contrast to the more accurate correlated levels and shows that even the fourth-order perturbation expansion is inadequate for this reaction.

Another potential source of problems with unrestricted MollerPlesset perturbation theory is spin contamination. Substantial spin contamination can cause errors of $5-15 \mathrm{kcal} / \mathrm{mol}$ in barrier heights. ${ }^{27}$ Thus, a second working hypothesis is that spin contamination is the source of the anomaly. Spin projection can be used to remove the effects of the unwanted spin states. As can be seen from Figure 8, spin projection deepens the well when cross sections at the PMPn levels are compared to the UMPn

[^2]

Figure 8. Spin projected MPn potential energy curves along the approximate MP2/6-31G** reaction path.


Figure 9. Potential energy curves calculated at (a) ROHF/6-31G** and (b) ROMP2/6-31G** along the approximate MP2/6-31G** reaction path. Note that the upper ROHF state corresponds to the lower ROMP2 state.
levels (tempting one to conclude that spin projection does not work, but see below). An alternate way to overcome the problems of spin contamination in the unrestricted Moller-Plesset perturbation theory is to use a restricted open shell (ROHF) reference wave function and include electron correlation corrections by restricted open shell MP2 theory (ROMP2). ${ }^{25}$ The ROHF and ROMP2 energy profiles are shown in Figure 9. The ROHF ground state wave function has broken spatial symmetry. The corresponding ROMP2 potential energy curve is higher than the UMP2 curve and also shows a less pronounced well centered around the $C_{20}$ symmetry structure. The spatially symmetric ${ }^{2} B_{2}$ ROHF state at the $C_{20}$ geometry lies above the crossing of the broken symmetry states. The corresponding ROMP2 energy is substantially lower than the broken symmetry ROMP2 energy curve. In fact, the ${ }^{2} B_{2}$ ROMP2 energy is similar to the projected UMP2 (PMP2) energy for the $C_{20}$ structure, indicating that spin projection is changing the energy in the correct direction. The ${ }^{2} B_{2}$ ROHF and ROMP2 surfaces, however, can be followed for

Scheme I

only a short distance from the $C_{20}$ structure before SCF convergence problems become overwhelming. Since the shallow well persists with a reference wave function free of spin contamination, spin contamination cannot be the source of the anomalous behavior of the MP2 surface. Because of symmetry breaking, the ROHF and ROMP2 approaches do not provide a satisfactory way around the UMP2 difficulties. Nevertheless, the presence of the broken symmetry states suggests a reexamination of the UHF surface for analogous states.

The origin of the broken symmetry states can be seen best by examining the linear structure. The three $\sigma$ orbitals involved in the making and breaking of the bonds and the $\pi$ lone pairs are sketched in Scheme I. The spatially symmetric configuration has the expected three $\sigma$ electrons and is denoted structure 1 , while the two broken symmetry configurations can be formed by removing an electron from the $\pi$ lone pair of one fluorine atom and placing it into the $\sigma$ orbitals. The $\sigma$ orbitals can localize into an $\mathrm{H}-\mathrm{F}$ bond and a fluorine $\sigma$ lone pair that interact via a hydrogen bond (structure 2a). The complementary broken symmetry state, structure $\mathbf{2 b}$, is formed by taking the electron from the other fluorine atom. At the linear geometry the $\sigma$ state and the broken symmetry $\pi$ states cannot interact. As can be seen in Figure 10, the curves cross and the broken symmetry $\pi$ states become lower for an antisymmetric displacement of $0.05 \AA$.

The correlation corrections calculated at the MP2 level are quite different for the symmetric state and the two broken symmetry states (see Figure 10b). Not surprisingly, the symmetric state that describes the making and breaking of the $\sigma$ bonds has a larger value of $E_{2}$; the broken symmetry states describe an elongated $\mathrm{H}-\mathrm{F}$ bond hydrogen bonded to a lone pair of the other fluorine and have a significantly smaller $E_{2}$. In the linear geometry, the states are of different symmetry, hence there is no difficulty arising from an avoided crossing.

When the linear structure is bent the four broken symmetry $\pi$ states split into two groups: one pair has the odd electron in a plane perpendicular to the FHF nuclear framework plane ( $A^{\prime \prime}$ state in $C_{s}$ point group) and the other pair has the odd $\pi$ electron in the plane ( $A^{\prime}$ state in $C_{s}$ point group). The $A^{\prime}$ states are of the same symmetry as the ground state and can interact with it. At an angle of $165^{\circ}$ and antisymmetric bond length displacements of $0.05 \AA$ or greater, the ground state UHF wave function is dominated by the broken symmetry wave function. The MP2 electron correlation energy is greater for the bond making/ breaking state than for the broken symmetry state as can be seen in Figure 11b. With a small amount of bending the crossing between the two UHF states is weakly avoided and the transition from the strongly correlated state 1 to the less correlated state $\mathbf{2}$ is abrupt. As bending increases the interaction becomes larger and the transition becomes smoother until all that remains is two small bumps separated by a small depression; this is depicted in Figure 12. This is the origin of the shallow depression on the


Figure 10. Potential energy curves calculated at (a) UHF/6-31G** and (b) UMP2/6-31G** along a collinear MP2/6-31G** reaction path.


Figure 11. Potential energy curves calculated at (a) UHF/6-31G** and (b) UMP2/6-31 $\mathrm{G}^{* *}$ along a reaction path with the $\mathrm{F}-\mathrm{H}-\mathrm{F}$ angle fixed at $165^{\circ}$.

MP2 surface. The increased interaction for the nonlinear geometry lowers the energy and hence is responsible for the bent geometry of the transition state. The strong interactions between


Figure 12. Potential energy curves calculated at the UMP2/6-31G** level along a reaction path with the $\mathrm{F}-\mathrm{H}-\mathrm{F}$ angle fixed at various values.
state 1 and state 2 suggest that a proper treatment of the electronic structure of this system may require CAS-SCF.

States 1 and 2 formally differ by a single excitation (Scheme I). The CISD, QCISD, QCISD(T), and CCSD calculations appear to handle this interaction properly. However, the MP2, MP3, and CCD methods which do not include single excitations perform rather poorly. The proper means of handling strong interactions between states, i.e. non-dynamic correlation, is multiconfiguration SCF. A small CAS-SCF/6-31G** calculation capable of describing the $\mathrm{H}-\mathrm{F}$ bond making and breaking process would include 3 electrons in 3 orbitals: $\sigma$ bonding ( $\sigma$ ), sigma nonbonding ( $\sigma^{\mathrm{nb}}$ ), and $\sigma$ antibonding ( $\sigma^{*}$ ) (corresponding to orbitals 5, 9, and 11 in Figure 4a). With the 6-31G** basis set the 3 electron 3 orbital CAS-SCF yielded a linear $D_{\infty h}$ transition state. However, a larger CAS-SCF/6-31G** calculation with 7 electrons and including the occupied and unoccupied in-plane $\pi$ and $\pi^{*}$ lone pair-like orbitals along with the $\sigma, \sigma^{\text {nb }}$, and $\sigma^{*}$ orbitals yielded a highly bent $C_{2 v}$ symmetry transition state ( $\angle \mathrm{FHF}$ $=132^{\circ}$ ). Both CAS-SCF structures have one imaginary frequency, indicating they are true transition states. The agreement between the large CAS-SCF calculation and the QCI, CID, CISD, and CCSD transition states indicates that these methods are sufficient to handle the interaction with the broken symmetry states, whereas MPn and CCD levels of theory are not.

[^3]Secondly, the CASSCF calculations show that the bending in the transition is due to the interaction of the fluorine lone pairs with the partially formed/broken $\mathrm{H}-\mathrm{F} \sigma$ bonds. This type of interaction is normally termed hyperconjugation and is better known for its conformational effects in ground state molecules (e.g. the anomeric effect ${ }^{28}$ ).
The highly bent nature of the $\mathrm{F}+\mathrm{HF}$ transition state is probably the reason that no structure is seen in the photodetachment spectra of FHF-. The FHF-ion is linear and would have very poor FrankCondon overlap with the highly bent F-H-F transition state. By contrast, the $\mathrm{Cl}-\mathrm{H}-\mathrm{Cl}$ transition state is closer to linear and has good overlap with $\mathrm{Cl}-\mathrm{H}-\mathrm{Cl}^{-}$, giving rise to the observed spectral features. ${ }^{2}$

## Conclusion

The transition state for $\mathrm{F}+\mathrm{HF}$ was found to be a highly bent, $C_{20}$ structure $\left(R(\mathrm{HF})=1.102 \AA, \angle \mathrm{~F}-\mathrm{H}-\mathrm{F}=134.6 \AA, E_{\text {rel }}=17.5\right.$ $\mathrm{kcal} / \mathrm{mol}$ at the QCISD(T)/D95 ++ (3df,2p) level). The MP2/ $6-31 G^{* *}$ potential energy surface contains a disturbing anomaly: instead of a transition state at $C_{20}$ geometry, one finds a shallow depression. At higher levels of theory, this artifact disappears. The weakly bound complex at the MP2 level is not the result of a strong interaction with a higher state at the $C_{2 v}$ geometry, nor is it the result of spin contamination. The source of the problem lies with the pair of $C_{s}$ transition states that flank the $C_{2 v}$ complex at the MP2 level. These are residuals of avoided crossings between the bond making/breaking state and two broken symmetry, hydrogen bonding states. These broken symmetry states are formally single excitations from a fluorine lone pair into the $\sigma$ non-bonding orbital. Higher levels of calculation that include single excitations in an iterative or self consistent fashion, rather than perturbative, treat this avoided crossing properly and thus do not have anomalous $C_{s}$ transition states and a $C_{20}$ minimum. The strong stabilizing interactions (i.e., hyperconjugation) between the fluorine lone pairs and the $\sigma$ orbitals involved in bond making/breaking are also responsible for the highly bent geometry of the transition structure.

Acknowledgment. We would like to thank the National Science Foundation for financial support (Grant No. CHE 90-20398) and the Pittsburgh Supercomputing Center and Cray Research for generous grants of computer time.


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